

Quick Sort

```
int partition(int[] A, int lower, int upper)
//@requires 0 <= lower && lower < upper && upper <=
\length(A);
//@ensures lower <= \result && \result < upper;
//@ensures gt(A[\result], A, lower, \result);
//@ensures leq(A[\result], A, \result+1, upper);
{
    int pivot_index = lower+(upper-lower)/2;
    int pivot = A[pivot_index];
    swap(A, pivot_index, upper-1);
    int left = lower;
    int right = upper-1;
    while (right > left)
        //@loop_invariant lower <= left && left <= right && right
        < upper;
        //@loop_invariant gt(pivot, A, lower, left);
        //@loop_invariant leq(pivot, A, left, right);
        //@loop_invariant pivot == A[upper-1];
        {
            if (pivot <= A[right])
                {
                    right--;
                }
            else
                {
                    swap(A, left, right);
                    left++; right--;
                }
        }
    swap(A, left, upper-1);
    return left;
}
```

```
void qsort(int[] A, int lower, int upper)
//@requires 0 <= lower && lower <= upper && upper <=
\length(A);
//@ensures is_sorted(A, lower, upper);
{
    if (upper-lower <= 1) return;
    int i = partition(A, lower, upper);
    qsort(A, lower, i);
    qsort(A, i+1, upper);
    return;
}
```

```
swap(A, pivot_index, upper-1);
int left = lower;
int right = upper-1;
while (right > left)
//@loop_invariant lower <= left && left <= right && right < upper;
//@loop_invariant gt(pivot, A, lower, left);
//@loop_invariant leq(pivot, A, left, right);
//@loop_invariant pivot == A[upper-1];
{
    ...
}
```

Binary Search

```
int bsearch(int x, int[] A, int n)
//@requires 0 <= n && n <= \length(A);
//@requires is_sorted(A, n);
/*@ensures (-1 == \result && !is_in(x, A, n))
|| ((0 <= \result && \result < n) && A[\result] == x); @*/
{
    int lo = 0;
    int hi = n;
    while (lo < hi)
        //@loop_invariant 0 <= lo && lo <= hi && hi <= n;
        //@loop_invariant (lo == 0 || A[lo-1] < x);
        //@loop_invariant (hi == n || A[hi] > x);
        {
            int mid = lo + (hi-lo)/2;
            //@assert lo <= mid && mid < hi;
            if (A[mid] == x) return mid;
            else if (A[mid] > x) hi = mid;
            else //@assert A[mid] < x;
                lo = mid+1;
        }
    return -1;
}
```

Linked Lists

```
struct list {
    string data;
    struct list next;
};
typedef struct list* list
```

Safe Add

$x + (y - x) / 2$

Overflow

assert(maxint - x > y)

Two's Complement of x

$\sim x + 1$

Min/Max

8 bit	-128	127
16 bit	-32768	32767
32 bit	-2147483648	2147483648

Big O

$f(n) = O(g(n))$ means there are positive constants c and k such that $0 <= f(n) <= cg(n)$ for all $n >= k$.

Complexity Proof

Prove that $3n^2 + n \log(n) + 6n + 6$ is $O(n^2)$

$3n^2 + n \log(n) + 6n + 6 <= cn^2$ for $c > 0, n >= n_0$

$3n^2 + n \log(n) + 6n + 6 <= 3n^2 + n^2 + n^2 + n^2$
 $= 6n^2$